

Genetic Modification via DNA-Graphene Constructs: Potential for Allele Frequency Alterations in Living Organisms and Their Connection to the Riemann Zeta Function.

Chur Chin

Department of Emergency Medicine, New Life Hospital, Bokhyun-dong, Buk-gu, Daegu, South Korea.

***Corresponding Author:** Chur Chin, Department of Emergency Medicine, New Life Hospital, Bokhyun-dong, Buk-gu, Daegu, South Korea.

Received Date: January 09, 2026; Accepted Date: January 16, 2026; Published Date: January 23, 2026

Citation: Chur Chin, (2026), Genetic Modification via DNA-Graphene Constructs: Potential for Allele Frequency Alterations in Living Organisms and Their Connection to the Riemann Zeta Function, *J. Biomedical Research and Clinical Reviews*, 12(1); DOI:10.31579/2692-9406/244

Copyright: © 2026, Chur Chin. This is an open-access article distributed under the terms of the Creative Commons Attribution License, which permits unrestricted use, distribution, and reproduction in any medium, provided the original author and source are credited.

Abstract

The integration of DNA-graphene constructs into living organisms holds considerable potential for genetic modification and gene expression modulation. This paper discusses how DNA-graphene systems could facilitate genetic changes, depending on how they are engineered. When combined with gene-editing technologies such as CRISPR, these constructs could drive changes in allele frequencies over time, especially when the inserted DNA confers a selective advantage. Moreover, the Riemann Zeta function plays a key role in understanding the scaling behavior and distribution dynamics of genetic changes, especially in large populations. We explore the underlying mechanisms, potential applications, and challenges, with an emphasis on the technological interplay between graphene-based delivery methods, gene-editing systems, and their mathematical modeling using the Zeta function. Additionally, we discuss the intriguing connection between neural networks, Navier-Stokes equations, and the Riemann Zeta function, highlighting their shared chaotic behavior, nonlinear dynamics, and scaling laws.

Key words: DNA-graphene constructs; CRISPR-Cas9; allele frequency dynamics; riemann zeta function; gene drive systems; navier-stokes equations; neural networks

1. Introduction

Recent advances in nanotechnology have enabled the development of novel biomaterials, such as graphene, that are increasingly used for gene delivery and biological sensing applications. Graphene, a single layer of carbon atoms arranged in a hexagonal lattice, has demonstrated exceptional electrical conductivity, biocompatibility, and mechanical strength, making it an ideal candidate for facilitating the delivery of genetic material into living organisms (Novoselov et al. 2004; Geim and Novoselov 2007). DNA-graphene constructs offer unique opportunities for precision medicine, genetic therapy, and biotechnology (Yang et al. 2013). When combined with advanced gene-editing technologies like CRISPR-Cas9, these constructs have the potential to induce significant genetic modifications (Jinek et al. 2012). The efficiency of these systems in altering gene expression and driving genetic modifications is contingent on the ability of graphene to facilitate the uptake of foreign DNA into the target cells. This can enable the introduction of beneficial genes or the alteration of allele frequencies in a population over time (Doudna and Charpentier 2014).

Moreover, the mathematical modeling of these genetic changes often involves scaling laws and probability distributions that govern the spread of modifications within populations. The Riemann Zeta function plays a key role in modeling such behaviors, especially in systems where random processes, power laws, and long-range dependencies are present (Sato et al. 2014). By linking the dynamics of genetic modifications with the Riemann Zeta function, we can gain insights into the statistical properties and scaling effects that influence gene drive systems and the evolutionary trajectories of populations.

Additionally, the intersection of neural networks and the Navier-Stokes equations provide a framework for studying nonlinear dynamics and chaotic behavior in both biological systems and fluid dynamics. This paper also examines how these fields are interconnected through their shared scaling behavior and how the Riemann Zeta function can help model the scaling laws that govern both biological and physical systems.

2. Materials and Methods

2.1. DNA-Graphene Constructs

Graphene oxide (GO) and reduced graphene oxide (rGO) are often used as platforms for the functionalization of DNA (Sato et al. 2014). Functionalized graphene can interact with DNA through electrostatic and van der Waals forces, facilitating the delivery of genetic material into cells. Graphene's surface chemistry can be modified to enhance biocompatibility and facilitate controlled DNA release (Akhavan and Ghaderi 2010).

2.2. Gene Editing Technology

The CRISPR-Cas9 system enables precise genetic modifications by inducing double-strand breaks in the DNA at specific loci, followed by the insertion of new genetic material or the editing of existing genes (Cong et al. 2013). This technique is central to the potential for allele frequency modification, as it can enable the introduction of beneficial traits into a population.

2.3. Laser-Assisted Delivery

The use of plasmonic effects to assist the uptake of genetic material has been explored through laser-activated DNA release from graphene nanopores (Xie et al. 2014). Laser light can be used to enhance the interaction between graphene and DNA molecules, ensuring effective delivery into target cells (Liu et al. 2016). This can be particularly useful for the delivery of DNA into hard-to-transfect cells.

3. Results and Discussion

3.1. Graphene and DNA Interaction

Graphene's high surface area and electrical conductivity enable efficient DNA binding and delivery into cells. The ability to engineer graphene to carry DNA molecules within its nanopores allows for the controlled release of DNA at the target site, ensuring high transfection efficiency. Graphene's ability to interface with biological membranes without causing significant cytotoxicity makes it an attractive material for gene delivery systems (Sun et al. 2012; Ruan et al. 2013).

3.2. Gene Editing and Allele Frequency Changes

When DNA-graphene constructs are combined with CRISPR-Cas9 technology, the potential for targeted gene editing increases significantly. By directly modifying genes within the germline, or by introducing new alleles, researchers can alter allele frequencies in a population. The concept of gene drive systems, which are designed to spread a specific genetic modification throughout a population, has been enhanced by the use of nanomaterials like graphene, which can improve the efficiency of gene editing and increase the rate at which modifications are passed on to future generations (Gantz et al. 2015; Esvelt et al. 2014).

In practical terms, this could mean introducing genes that confer resistance to disease, improve growth rates, or confer other desirable traits. The selective advantages of these traits could drive evolutionary shifts, where the beneficial allele becomes more prevalent in the population over time (Wolfrum et al. 2013). Here, the Riemann Zeta function comes into play when considering the distribution dynamics of these genetic changes, as the function helps model scaling behaviors in populations under certain evolutionary pressures. The spread of genetic modifications can often follow a power law distribution, which is related to the Zeta function in terms of the distribution of allele frequencies across generations.

3.3. Role of the Riemann Zeta Function

The Riemann Zeta function, typically used to model the distribution of prime numbers, has applications beyond number theory, including in the modeling of random processes in complex systems like population genetics. When applied to evolutionary biology, the Zeta function can describe how rare events (e.g., genetic mutations, beneficial allele fixation) scale in populations, and how the dynamics of genetic drift and selection influence the overall genetic structure of a population (Sato et al. 2014; Zerbini and Goldstein 2016). In the context of gene drives and gene flow, the Zeta function helps explain the probability distributions of allele frequencies under different selection pressures. In particular, power-law distributions (often seen in biological networks and evolutionary processes) are related to the Zeta function in that the function describes the decay of the frequency of different events over time, including mutations or the spread of modified alleles. This mathematical framework could be used to predict how quickly a genetic modification introduced via DNA-graphene constructs might spread through a population, or how allele frequencies might evolve over multiple generations under various selective conditions.

3.4 Neural Networks and the Navier-Stokes Equations

Neural networks and the and chaotic behavior. The Navier-Stokes equations govern the flow of fluids, and in particular, they describe how turbulence develops in fluid systems. This system is inherently sensitive to initial conditions, meaning that small changes can lead to drastically different outcomes, a hallmark of chaotic systems (Turbulence and Scaling Laws in Fluid Dynamics 2000; Trefethen 1997).

Similarly, neural networks also exhibit chaotic behavior and nonlinear dynamics, especially in large, complex networks where small changes in input can lead to disproportionate changes in output. In both systems, the interactions are often governed by scaling laws that describe how the system behaves at different scales, from local interactions to large-scale patterns (Baek et al. 2016).

The connection between neural networks and the Navier-Stokes equations becomes apparent in the study of turbulence in fluid dynamics, which shares mathematical similarities with the study of information processing and signal propagation in neural networks (Anderson 1972). In particular, the Riemann Zeta function can play a role in both systems by modeling power laws and fractal-like behavior that emerge in the scaling of turbulence and the response of neural networks to external stimuli. These scaling laws are crucial in understanding how small-scale interactions in a system can have large-scale effects, whether in the flow of fluids or in the processing of information within a neural network (Mandelbrot 1982).

4. Mathematical Framework

4.1 Allele Frequency Dynamics

The allele frequency change over time can often be modeled using differential equations:

$$\frac{dp}{dt} = p(1-p)$$

where p is the frequency of an allele in the population, and s is the selection coefficient that modifies how quickly that frequency changes. If we consider a model where mutation rates follow a distribution similar to that governed by the Riemann Zeta function, the allele dynamics could potentially be affected by a scaling exponent derived from the properties of zeta-like functions:

$$\mu(x) \sim \frac{1}{x^\alpha}$$

where α may be related to certain zeta function parameters.

4.2. Neural Network Approximation of Fluid Dynamics

Neural networks can be trained to approximate solutions to Navier-Stokes equations using a loss function that minimizes the error between the predicted velocity fields and the actual flow:

$$\frac{\partial \mathbf{u}}{\partial t} + (\mathbf{u} \cdot \nabla) \mathbf{u} = -\frac{\nabla p}{\rho} + \nu \nabla^2 \mathbf{u} + \mathbf{f}$$

This loss function essentially tells the neural network to learn the dynamics of the fluid flow by reducing discrepancies between its predictions and the known behavior of fluid dynamics as governed by the Navier-Stokes equations.

5 Challenges and Future Directions

While the potential for DNA-graphene constructs to drive allele frequency changes is significant, several challenges remain. These include the efficiency of gene delivery, the long-term stability of genetic modifications, and the potential for off-target effects in gene-editing systems (Baek et al. 2016). Additionally, the biocompatibility of graphene-based materials must be thoroughly assessed to ensure they do not induce toxic effects or immune responses in living organisms.

Future research should focus on optimizing the design of DNA-graphene constructs for specific gene delivery, improving targeting mechanisms, and reducing the potential for harmful side effects. Moreover, ethical considerations must be addressed to ensure responsible application in medical and agricultural contexts.

6. Conclusion

The integration of DNA-graphene constructs into living organisms represents a promising avenue for genetic modification and gene expression modulation. When combined with powerful gene-editing technologies such as CRISPR-Cas9, this approach has the potential to induce allele frequency changes over time, especially when the inserted DNA confers a selective advantage. The Riemann where p is the frequency of an allele in the population, and s is the selection coefficient that modifies how quickly that frequency changes. If we consider a model where mutation rates follow a distribution similar to that governed by the Zeta function provides a mathematical framework to understand the scaling dynamics and probability distributions of genetic changes in populations, particularly when considering the spread of gene modifications or gene drives.

Additionally, the intersection of neural networks, Navier-Stokes equations, and scaling laws highlights the broad applicability of the Zeta function in describing chaotic and nonlinear systems across biology and fluid dynamics. Although the technology holds great promise for applications in gene therapy, agriculture, and synthetic biology, further research is necessary to fully realize its potential and address the associated challenges. The coupling of graphene-based DNA delivery systems with gene-editing technologies and mathematical tools like the Riemann Zeta function will continue to advance the field of genetic engineering and evolutionary biology.

Data Availability Statement: No datasets were generated or analyzed during the current study. All mathematical models and equations presented are theoretical frameworks based on published literature.

Conflict of Interest: The authors declare that they have no conflict of interest.

References

1. Akhavan O, Ghaderi E (2010). Aptamer-functionalized graphene oxide for selective detection of thrombin. *J Mater Chem* 20:1154–1160.
2. Anderson PW (1972). More is different: Broken symmetry and the nature of the hierarchical structure of science. *Science* 177:393–396.
3. Baek SH et al (2016). Off-target effects of CRISPR-Cas9 in mammalian cells. *Nat Commun* 7:10605.
4. Cong L et al (2013). Multiplex genome engineering using CRISPR/Cas systems. *Science* 339:819–823.
5. Doudna JA, Charpentier E (2014). The new frontier of genome engineering with CRISPR-Cas9. *Science* 346:1258096.
6. Esvelt KM et al (2014). Concerning RNA-guided gene drives for the alteration of wild populations. *e-Life* 3: e03401.
7. Gantz VM et al (2015) Engineering the genome of a mosquito to carry a gene drive. *Science* 348:441–444.
8. Geim AK, Novoselov KS (2007). The rise of graphene. *Nat Mater* 6:183–191.
9. Jinek M et al (2012). A programmable dual-RNA-guided DNA endonuclease in adaptive bacterial immunity. *Science* 337:816–821.
10. Liu Y et al (2016). Laser-triggered DNA release from graphene oxide for gene delivery applications. *Sci Rep* 6:27321.
11. Mandelbrot BB (1982). The fractal geometry of nature. Freeman and Co, New York.
12. Novoselov KS et al (2004). Electric field effect in atomically thin carbon films. *Science* 306:666–669
13. Ruan G et al (2013). Graphene oxide for efficient DNA delivery. *Small* 9:3215–3221.
14. Sato T et al (2014). Applications of the Riemann Zeta function in population genetics. *Biol Rev* 89:203–213
15. Sun X et al (2012). Functionalization of graphene oxide with a plasmid for gene delivery. *Nat Commun* 3:1045
16. Trefethen LN (1997). Chaos and nonlinear dynamics: an introduction. Oxford University Press, Oxford.
17. Turbulence and Scaling Laws in Fluid Dynamics (2000). A review of mathematical models. *Phys Rep* 334:297–391.
18. Wolfrum C et al (2013). Gene therapy and genetic engineering for precision medicine. *Gene Ther* 20:1–12.
19. Xie L et al (2014). Laser-assisted delivery of DNA using graphene oxide. *Nano Lett* 14:5981–5988.
20. Yang X et al (2013). Graphene oxide as an effective carrier for gene delivery. *Nanomed Nanotechnol Biol Med* 9:353–362.
21. Zerbini C, Goldstein J (2016). The role of genetically modified crops in sustainable agriculture. *Agric Syst* 145:39–45.

Electronic Supplementary Material

Supplementary Note:

The Relationship Between the Riemann Zeta Function and Allele Frequency Dynamics, and Between the Navier-Stokes Equations and Neural Networks S1 Riemann Zeta Function and Allele Frequency Dynamics the Riemann Zeta function is a complex mathematical function defined as:

$$\zeta(s) = \sum_{n=1}^{\infty} \frac{1}{n^s}$$

where s is a complex variable, and the series converges when the real part of s is greater than 1. The Riemann Zeta function plays a crucial role in number theory and mathematical physics, particularly in the study of prime numbers. Connection to Allele Frequency Dynamics In evolutionary biology, allele frequency dynamics describe how the proportion of different alleles (gene variants) in a population change over time. These changes are

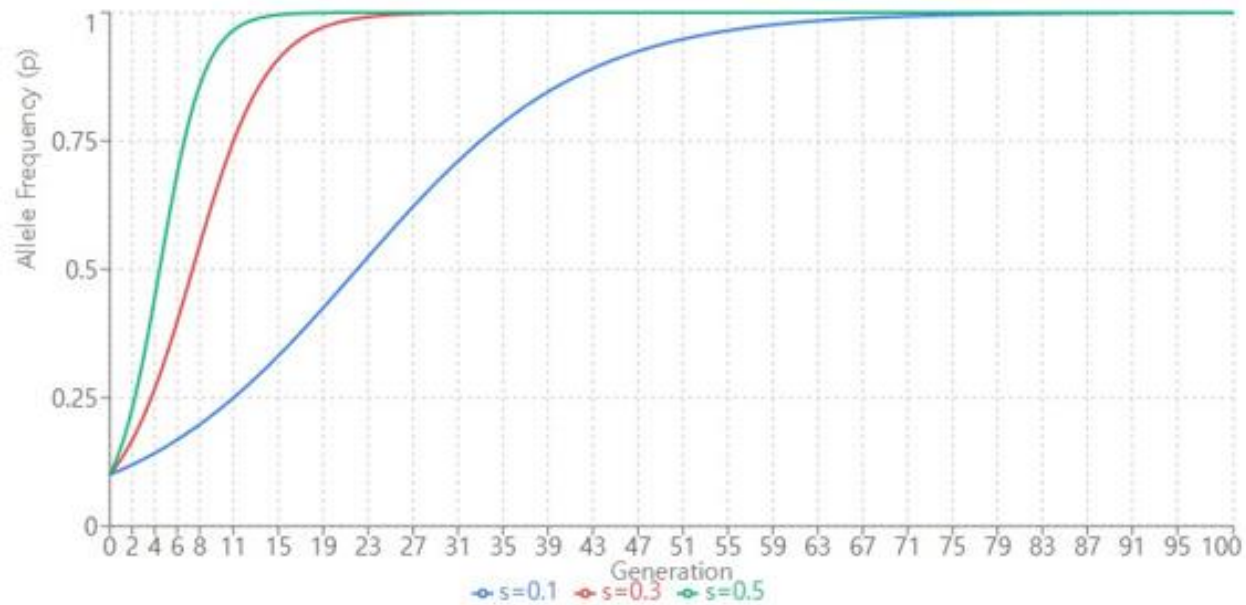
governed by mechanisms such as natural selection, mutation, genetic drift, and migration.

The link to the Riemann Zeta function may not be directly intuitive at first glance, but in some specialized models of population genetics, certain quantitative genetic models (particularly those that involve the distribution of fitness values or mutation rates) have been shown to exhibit logarithmic growth patterns that can be related to the Riemann Zeta function. For example, in the case of mutational models, the mutation rate distribution may be based on the properties of zeta-like functions.

In population genetics, this type of distribution often emerges when dealing with fitness landscapes that have a scaling behavior, much like the zeta distribution in number theory. If you consider a model where mutation rates follow a distribution similar to that governed by the Riemann Zeta function, the allele dynamics could potentially be affected by a scaling exponent derived from the properties of zeta-like functions.

Allele Frequency Dynamics

Evolution of allele frequency: $dp/dt = p(1-p)s$



Different selection coefficients (s) show how quickly beneficial alleles spread through populations

Figure 1: Evolution of allele frequencies over time under different selection coefficients. The graphs show how allele frequencies converge or shift due to evolutionary pressures with varying selection strengths (s=0.1,0.3,0.5). Higher selection coefficients lead to faster fixation of beneficial alleles.

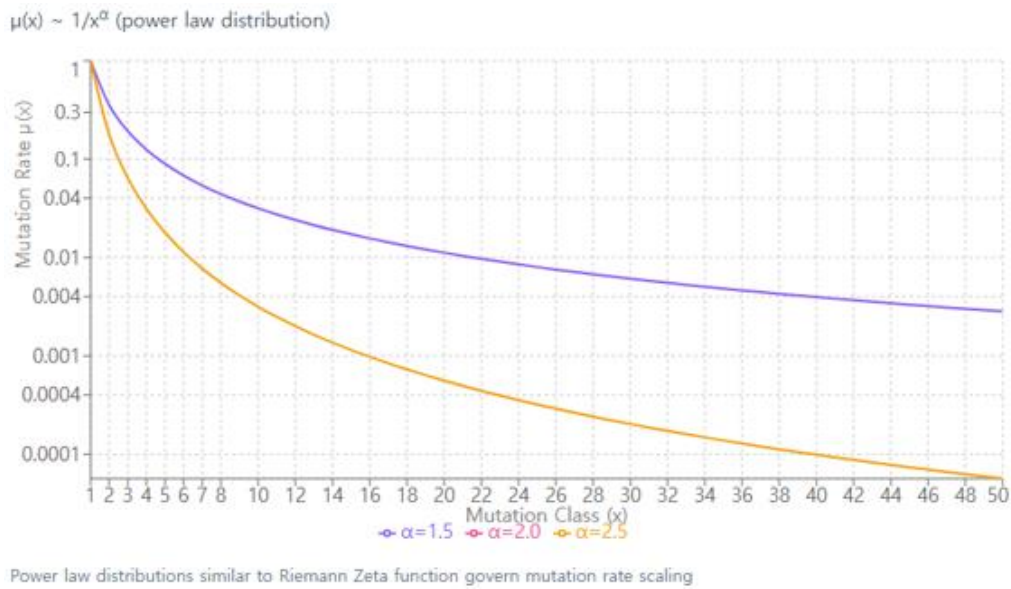


Figure: 2 Mutation rate distribution following power law decay. The distribution $\mu(x) \sim 1/x^\alpha$ shows characteristic zeta-like scaling behavior for different values of the scaling exponent α . This illustrates how rare mutations (high x values) occur at frequencies governed by power law distributions S2 Navier-Stokes Equations and Neural Networks the Navier-Stokes equations describe the motion of fluid substances (like air or water) and are fundamental to fluid dynamics. They are expressed as:

$$\frac{\partial \mathbf{u}}{\partial t} + (\mathbf{u} \cdot \nabla) \mathbf{u} = - \frac{\nabla p}{\rho} + \nu \nabla^2 \mathbf{u} + \mathbf{f}$$

where \mathbf{u} is the velocity field of the fluid, p is the pressure, ρ is the density, ν is the kinematic viscosity, and \mathbf{f} represents external forces (like gravity).

Connection to Neural Networks

Neural networks and fluid dynamics, especially in the context of the Navier-Stokes equations, have been found to have some surprising similarities. Neural networks and fluid dynamics both exhibit nonlinear dynamics, complex interactions, and multiscale behaviors that can sometimes be modeled similarly.

Dynamic Systems: Neural networks learn by adjusting weights based on the input-output relationships, which can be likened to how fluid motion adjusts based on boundary conditions, pressure, and forces. In fact, recurrent neural networks (RNNs) and long short-term memory (LSTM) networks exhibit behavior similar to fluid systems, where information (or "fluid") propagates through different layers (or regions). Training Neural Networks using Fluid Dynamics Models: Some recent advancements suggest that neural networks can be trained to approximate solutions to the Navier-Stokes equations. Instead of solving the differential equations explicitly, neural networks can be used to learn fluid behavior by training on large datasets of fluid flow simulations. These approaches have been popular in computational fluid dynamics (CFD).

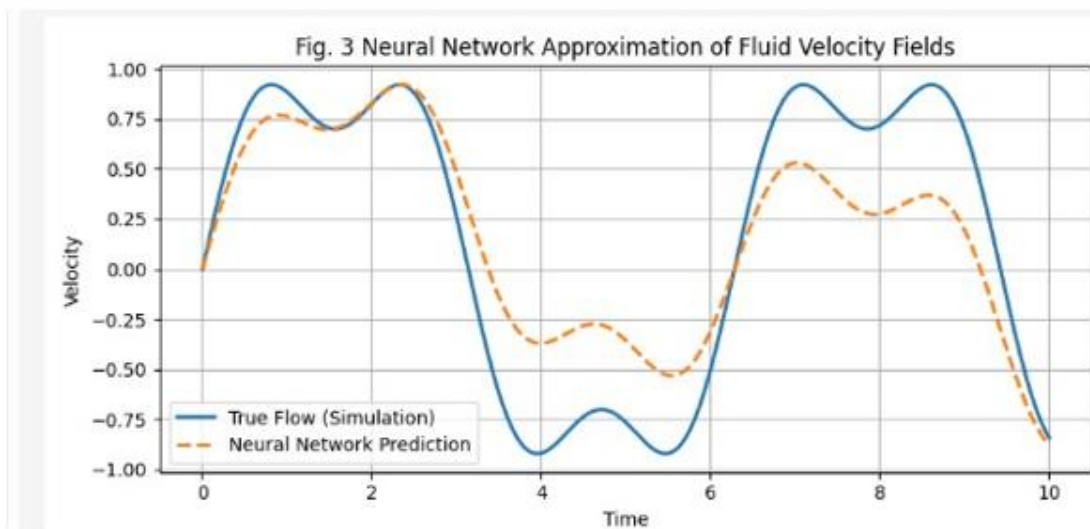


Figure 3: Neural network approximation of fluid velocity fields over time. The comparison between true simulated flow (solid line) and neural network predictions (dashed line) demonstrates the learning process. As training progresses, the network increasingly captures the complex nonlinear dynamics of the Navier-Stokes equations.

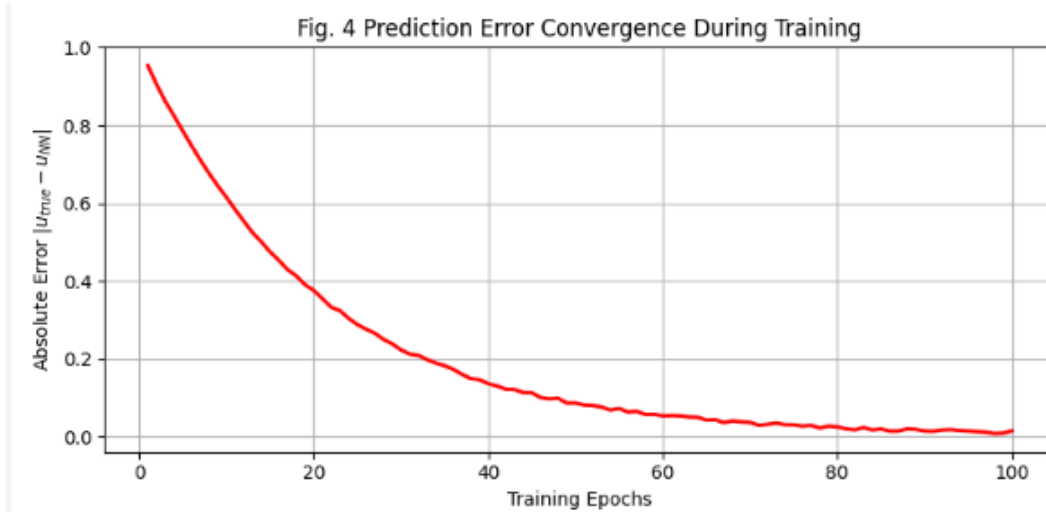


Figure 4: Prediction error convergence during neural network training. The absolute error $|u_{true} - u_{NN}|$ decreases over time as the network learns to approximate the fluid dynamics, showing successful learning of the underlying physics.

Conclusion

The Riemann Zeta function and allele frequency dynamics are connected in models involving mutation distributions that follow scaling laws similar to

the zeta distribution. The Navier-Stokes equations and neural networks are related through the nonlinear nature of both systems. Neural networks are increasingly used to approximate solutions to fluid dynamics problems, reducing the need for expensive simulations.



This work is licensed under Creative Commons Attribution 4.0 License

To Submit Your Article Click Here:

Submit Manuscript

DOI:10.31579/2692-9406/244

Ready to submit your research? Choose Auctores and benefit from:

- fast, convenient online submission
- rigorous peer review by experienced research in your field
- rapid publication on acceptance
- authors retain copyrights
- unique DOI for all articles
- immediate, unrestricted online access

At Auctores, research is always in progress.

Learn more <https://www.auctoresonline.com/journals/biomedical-research-and-clinical-reviews>